STOCHASTIK Rhein-Main

08.11.2022 Markus Schepers, Cover and Hitting Times of Hyperbolic Random Graphs



Oberseminar Mainz

Date: 08.11.2022 Time: 14:15-16:00 h

Number

160

Speaker

Markus Schepers, UniMedizin Mainz

Abstract: We study random walks on the giant component of Hyperbolic Random Graphs (HRGs), in the regime when the degree distribution obeys a power law with exponent in the range (2, 3). In particular, we focus on the expected times for a random walk to hit a given vertex or visit, i.e. cover, all vertices. We show that up to multiplicative constants: the cover time is n(log n)^2, the maximum hitting time is n log n, and the average hitting time is n. The first two results hold in expectation and a.a.s. and the last in expectation (with respect to the HRG). We prove these results by determining the effective resistance either between an average vertex and the well-connected "center" of HRGs or between an appropriately chosen collection of extremal vertices. We bound the effective resistance by the energy dissipated by carefully designed network flows associated to a tiling of the hyperbolic plane on which we overlay a forest-like structure. (joint work with Marcos Kiwi and John Sylvester)

Place

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Organizing partners

Technische Universität Darmstadt, Goethe-Universität Frankfurt am Main